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## Note on Waiting Lines: Variability, Utilization, and Inventory

## Introduction

All real-life service systems exhibit some degree of variability in both input process (inter-arrival times) and service process (service times). We observe those processes and describe them statistically in terms of their means  $(\boldsymbol{a}, \boldsymbol{p})$  and standard deviations  $(\boldsymbol{\sigma}_a, \boldsymbol{\sigma}_p)$ . With this information, and the number of service channels  $(\boldsymbol{m})$ , we can predict the expected steady-state wait time for service,  $\boldsymbol{T}_q$  – the average  $\boldsymbol{T}$  ime spent by an item in  $\boldsymbol{q}$  ueue waiting to be served. Using this information, and applying Little's Law which states that Inventory = Rate \* Time, we can compute other system performance measures for use in making system design and improvement decisions. So, by measuring and computing just 5 basic system values, we can predict with a high level of accuracy how the service system will perform in its base state, and how that performance will change in response to managerial actions.

"Waiting Lines: Variability, Utilization, and Inventory: Spreadsheet" (ID: 1-429-243) accompanies this note and can be used to learn more about the VUT equation, and to experiment with applying it to real-life service systems.

## Variability-Utilization-Service Time (VUT) Equation

## In words:

Average wait time for service endured by customers (or items) is determined by the product of three terms:

- A variability term computed from the squared coefficients of variation (standard deviation divided by the mean) of inter-arrival and service times
- A utilization term computed from inter-arrival and service times and the number of service channels
- And the average service time.

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